

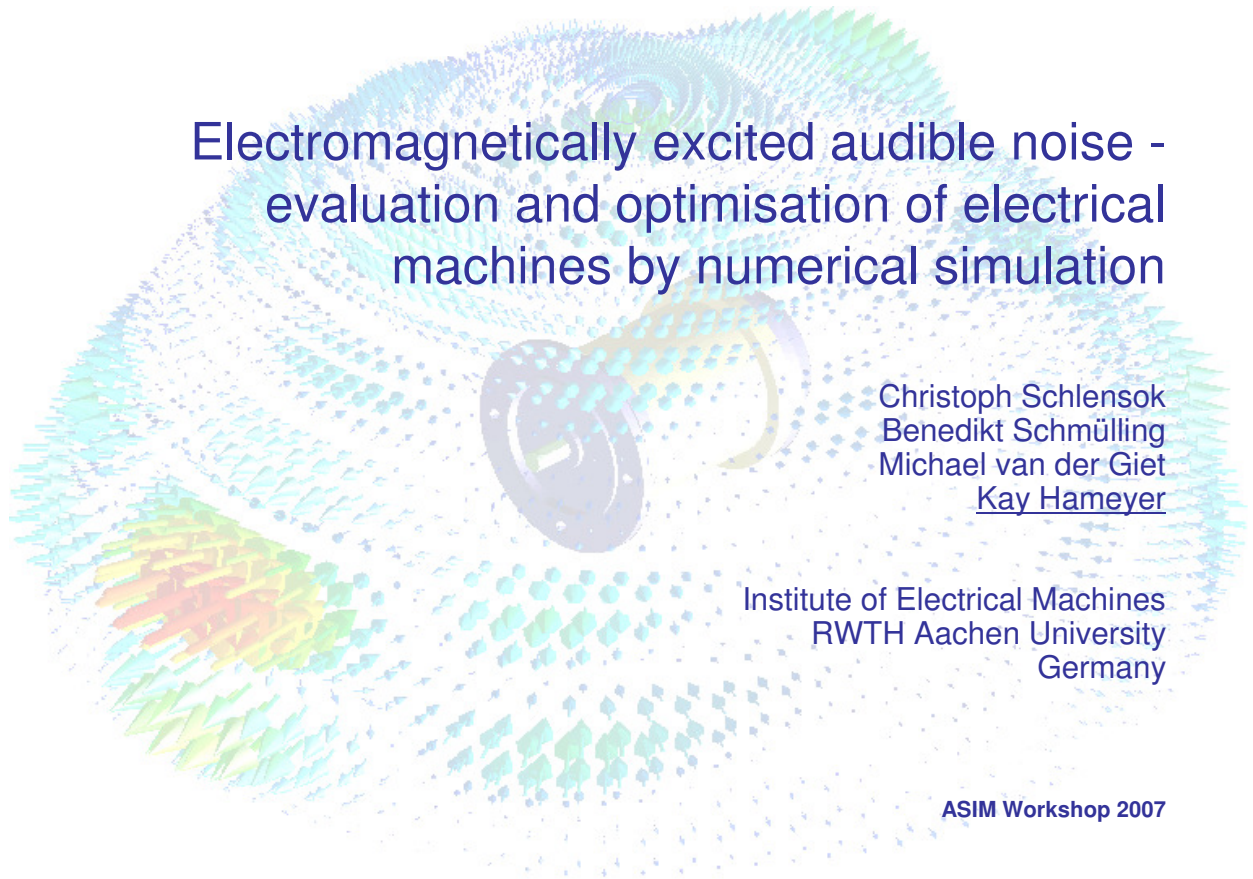


# Electromagnetically excited audible noise - evaluation and optimisation of electrical machines by numerical simulation

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Michael van der Giet  
Kay Hameyer

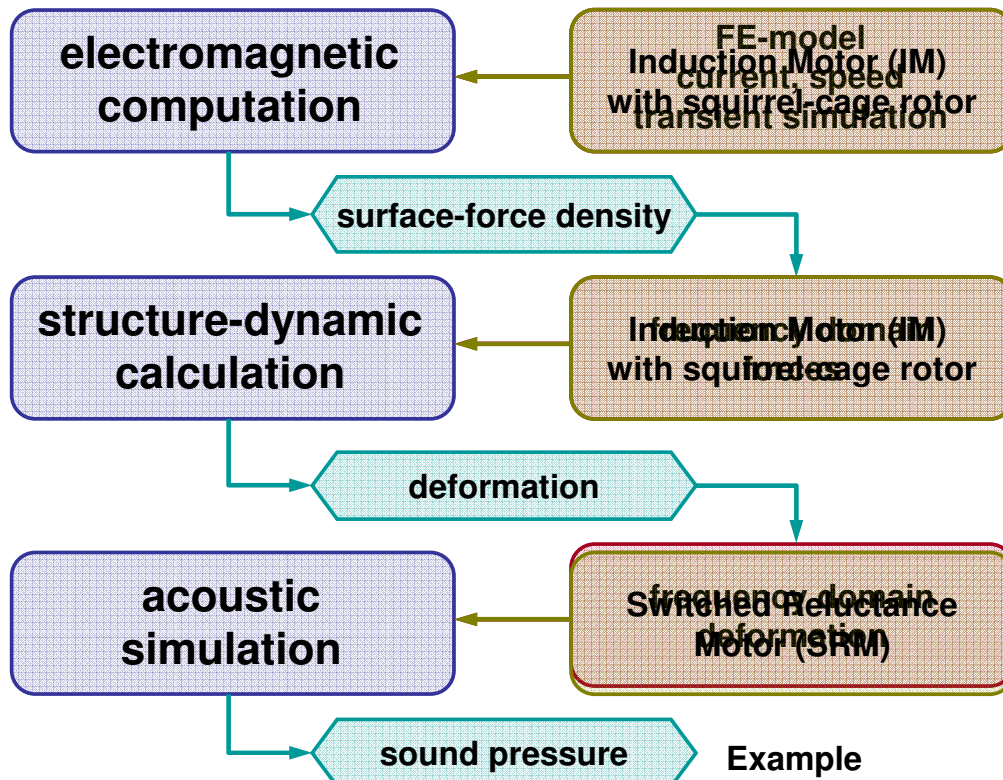
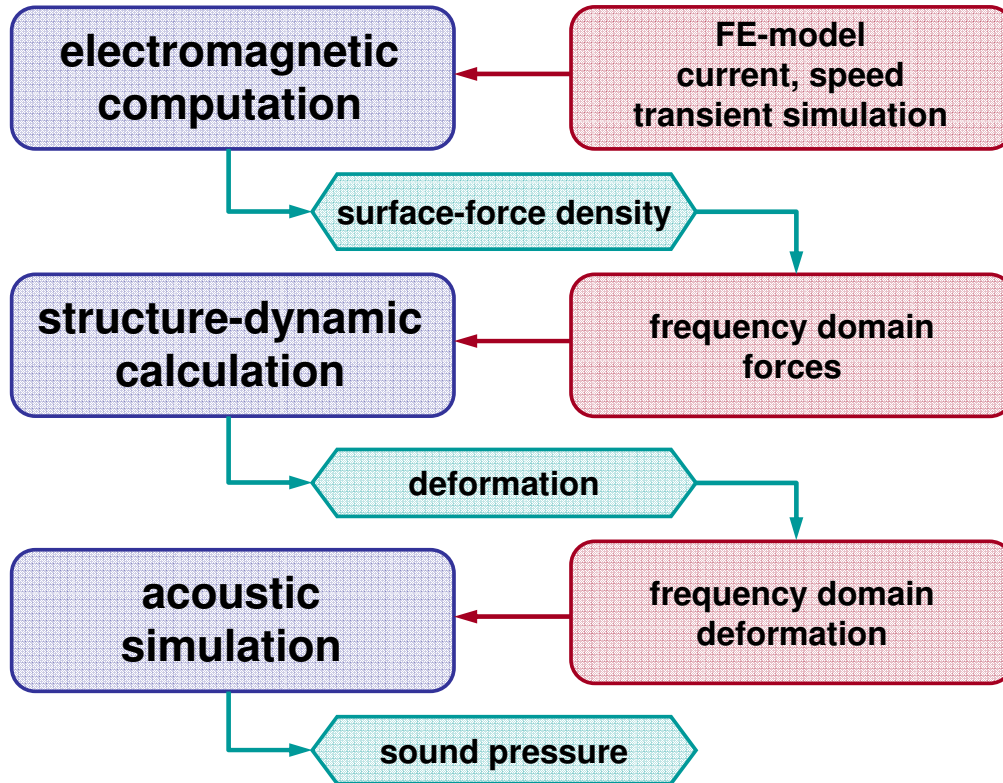
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ASIM Workshop 2007



## Outline

- Introduction
  - Problem description: Multi-physics
  - What are the tools
- Electro-magnetic computation
  - Modelling
  - Results
- Structure-dynamic calculation
  - Modelling
  - Results
- Acoustic simulation
  - Modelling
  - Results
- Conclusions



Example



# What are the tools: Analytical model

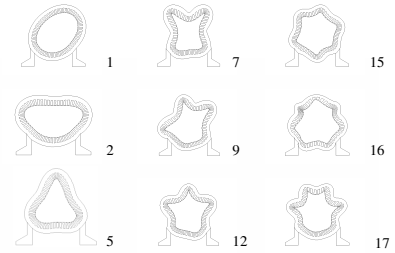


- Tables to determine the mechanical order and associated frequency regarding the source of the excitation
- Example:

Magnetische Anregungen für Geräusche bei Asynchronmaschinen (Käfigläufer):

Strangzahl m	3		Lochzahl q <sub>1</sub>	2
Polzahl 2p	6	--> p	3	
Frequenz f <sub>1</sub>	50			
Nutzahl N <sub>1</sub>	36			
N <sub>2</sub>	28			
Schlupf s	0			
Exzentrizität K	0			

K=0 für stst. Ex.  
K=1 für dyn. Ex.



Geräuschanregungen der Oberfelder des Ständers in dem Zusammenwirken mit den:

Läuferrestfelder des Grundstrombelages

Nutzharmische g <sub>1</sub> /q <sub>1</sub>	-0,5	0,5	-1	1	-1,5	1,5	-2	2	-2,5	2,5	-3	3	-3,5	3,5	-4	4	-4,5	4,5	-5	5	Frequenz [Hz]		
g <sub>1</sub>	0	-1	1	-2	2	-3	3	-4	4	-5	5	-6	6	-7	7	-8	8	-9	9	-10	10		
Wicklungsfelder	1	-5	7	-11	13	-17	19	-23	25	-29	31	-35	37	-41	43	-47	49	-53	55	-59	61		
g <sub>2</sub> nue <sub>1</sub>	3	-15	21	-33	39	-51	57	-69	75	-87	93	-105	111	-123	129	-141	147	-159	165	-177	183		
nue <sub>2</sub>																							
0	+	6	-12	24	-30	42	-48	60	-66	78	-84	96	-102	114	-120	132	-138	150	-156	168	-174	186	100
3	-	0	18	-18	36	-36	54	-54	72	-72	90	-90	108	-108	126	-126	144	-144	162	-162	180	-180	0
-1	+	-22	-40	-4	-58	14	-76	32	-94	50	-112	68	-130	86	-148	104	-166	122	-184	140	-202	158	-366,67
-25	-	-28	-10	-46	8	-64	26	-82	44	-100	62	-118	80	-136	98	-154	116	-172	134	-190	152	-208	-466,67
1	+	34	16	52	-2	70	-20	88	-38	106	-56	124	-74	142	-92	160	-110	178	-128	196	-146	214	566,667
31	-	28	46	10	64	-8	82	-26	100	-44	118	-62	136	-80	154	-98	172	-116	190	-134	208	-152	466,667
-2	+	-50	-68	-32	-86	-14	-104	4	-122	22	-140	40	-158	58	-176	76	-194	94	-212	112	-230	130	-833,33
-53	-	-56	-38	-74	-20	-92	-2	-110	16	-128	34	-146	52	-164	70	-182	88	-200	106	-218	124	-236	-933,33
2	+	62	44	80	26	98	8	116	-10	134	-28	152	-46	170	-64	188	-82	206	-100	224	-118	242	1033,33
59	-	56	74	38	92	20	110	2	128	-16	146	-34	164	-52	182	-70	200	-88	218	-106	236	-124	933,333
-3	+	-78	-96	-60	-114	-42	-132	-24	-150	-6	-168	12	-186	30	-204	48	-222	66	-240	84	-258	102	-1300
-81	-	-84	-66	-102	-48	-120	-30	-138	-12	-156	6	-174	24	-192	42	-210	60	-228	78	-246	96	-264	-1400
3	+	90	72	108	54	126	36	144	18	162	0	180	-18	198	-36	216	-54	234	-72	252	-90	270	1500
87	-	84	102	66	120	48	138	30	156	12	174	-6	192	-24	210	-42	228	-60	246	-78	264	-96	1400
-4	+	-106	-124	-88	-142	-70	-160	-52	-178	-34	-196	-16	-214	2	-232	20	-250	38	-268	56	-286	74	-1766,7
-109	-	-112	-94	-130	-76	-148	-58	-166	-40	-184	-22	-202	-4	-220	14	-238	32	-256	50	-274	68	-292	-1866,7

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# What are the tools: Numerical model



- Own software applied for entire simulation chain

## iMOOSE & iMOOSE.trinity

### Finite/Boundary Element Solvers and Tools



&



$$U_i = \oint_s \vec{E} \cdot d\vec{s} \quad \text{rot} \vec{A} = \vec{B}$$

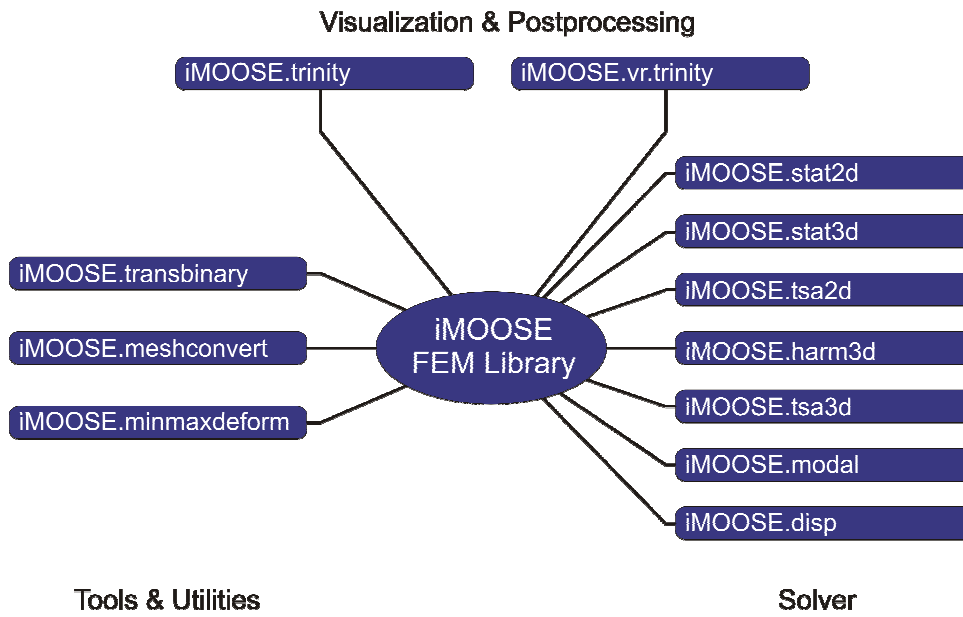
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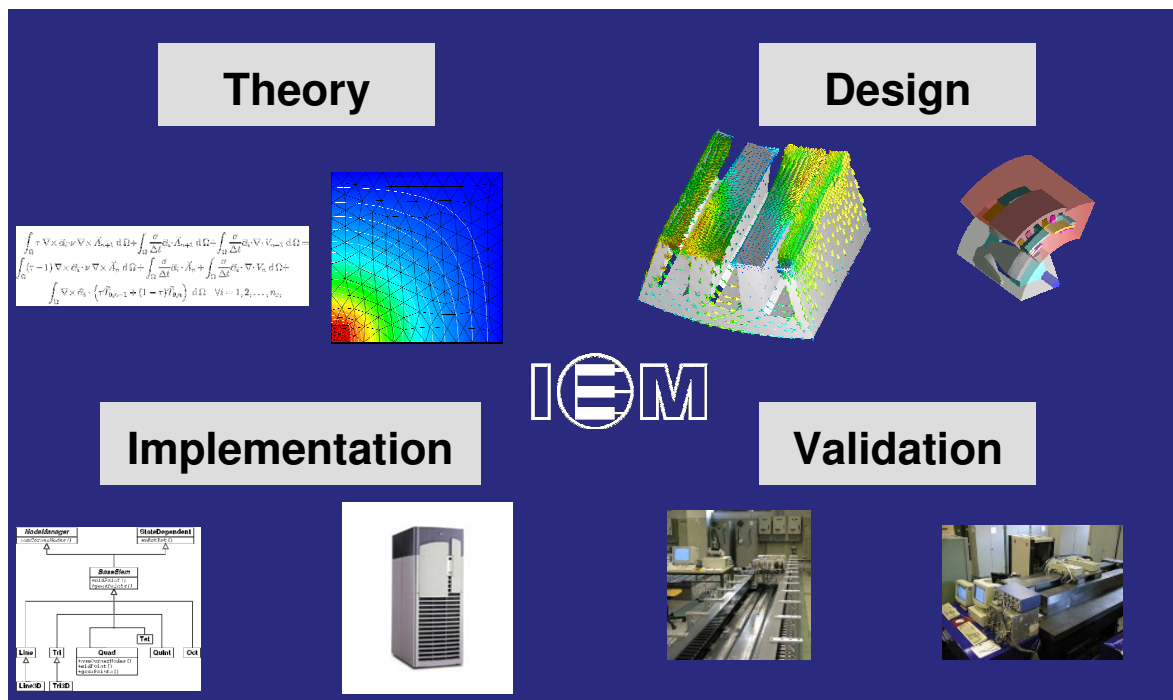
## ➤ iMOOSE – innovative and modern Object-Oriented Solver Environment



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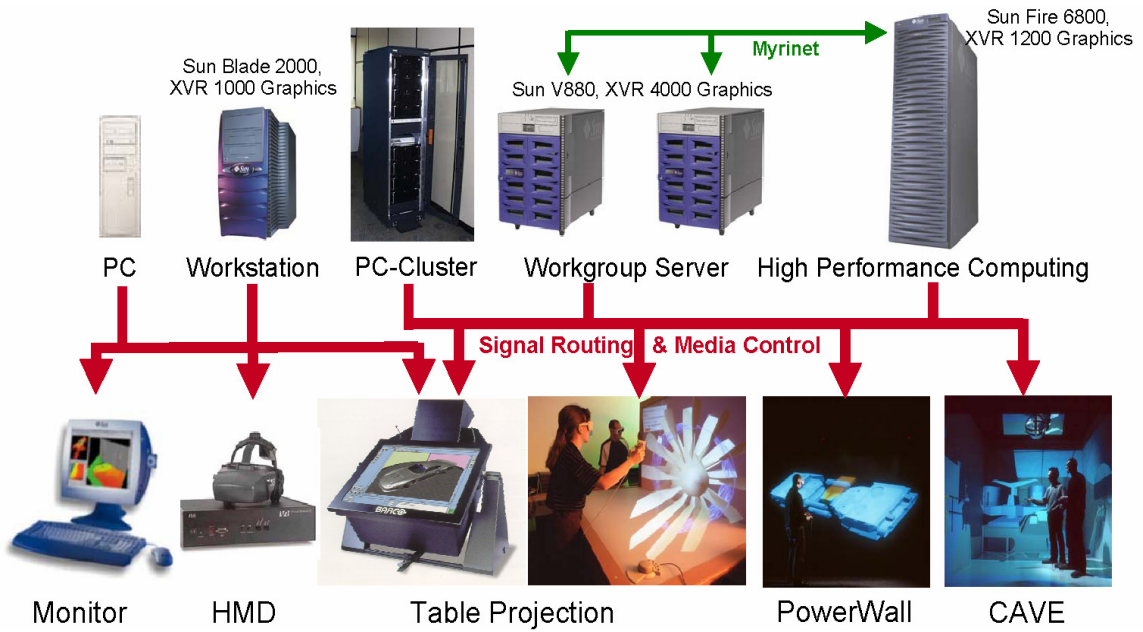


## ➤ Simulation & Design of Electrical Machines

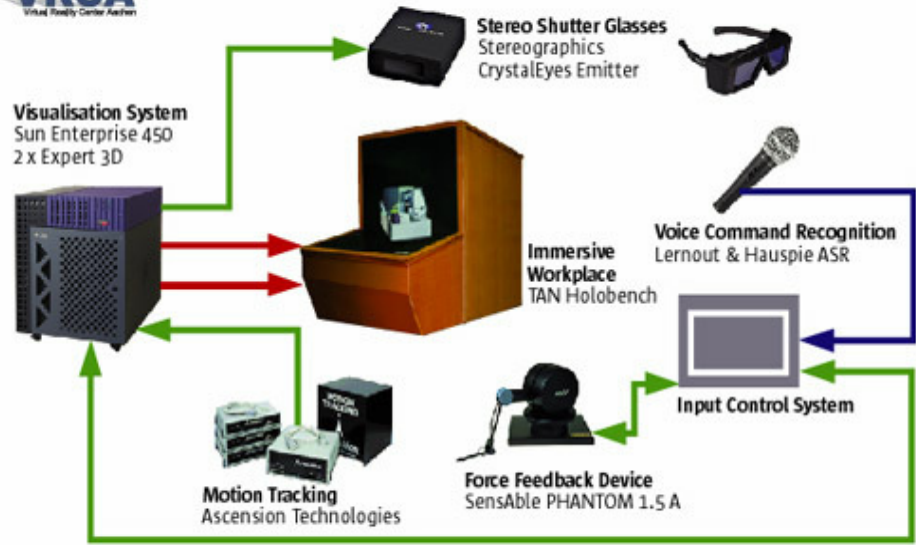


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Virtual Reality Center Aachen: Immersive Workplace Setup





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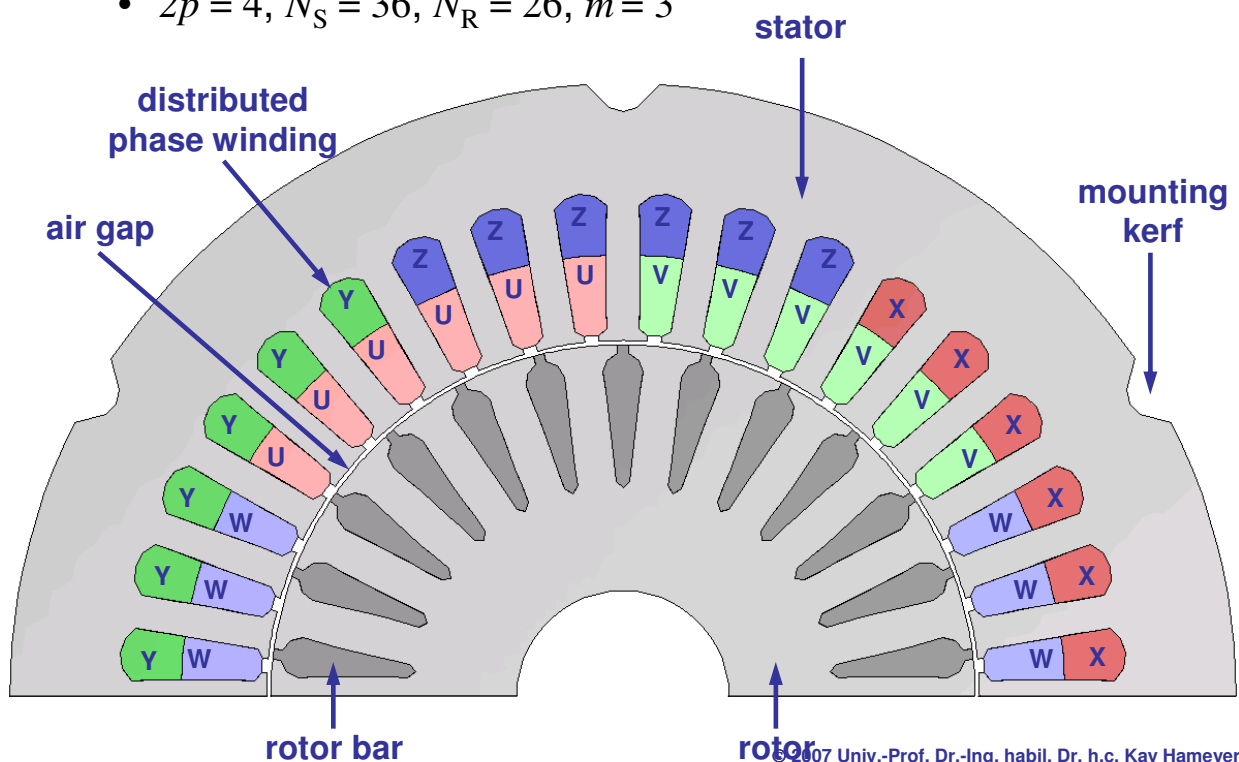
**electromagnetic computation**

**FE-model  
current, speed  
transient simulation**

- Modelling
    - 2D/3D possible in general  
⇒ 2D whenever possible, 3D requires huge computational cost
    - static, time harmonic, transient
    - with or without movement
  - This example: Induction Machine (IM) with squirrel-cage rotor
    - 2D, multi-slice model
    - transient simulation
    - rotor movement
- ⇒ transient phenomenon must die out before analysis of the simulation results can start

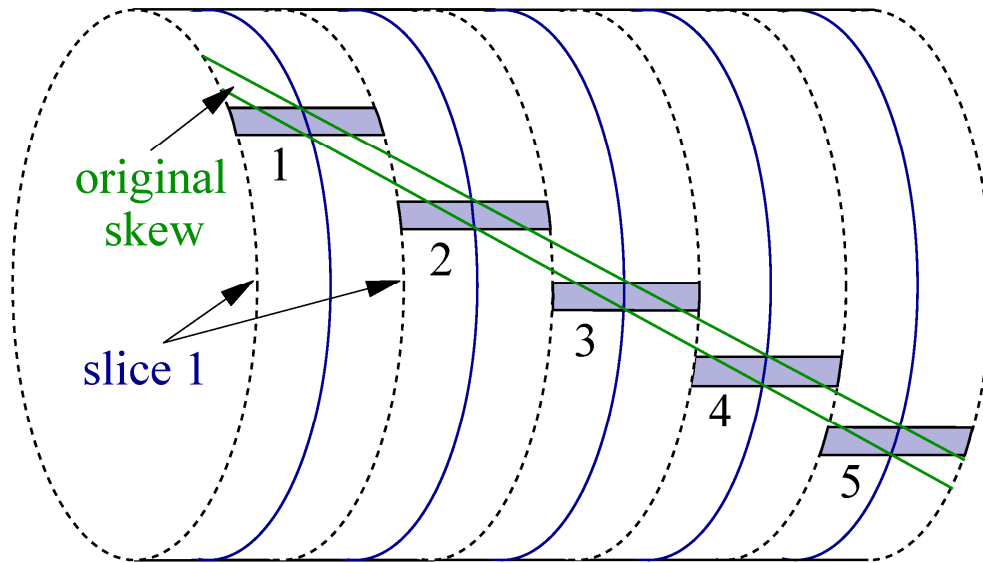


- Electromagnetic model of IM
  - $2p = 4, N_S = 36, N_R = 26, m = 3$





- Skew of the IM is modelled with multi-slice technique



- 5 models are coupled
  - each  $\approx 15.000$  triangular elements



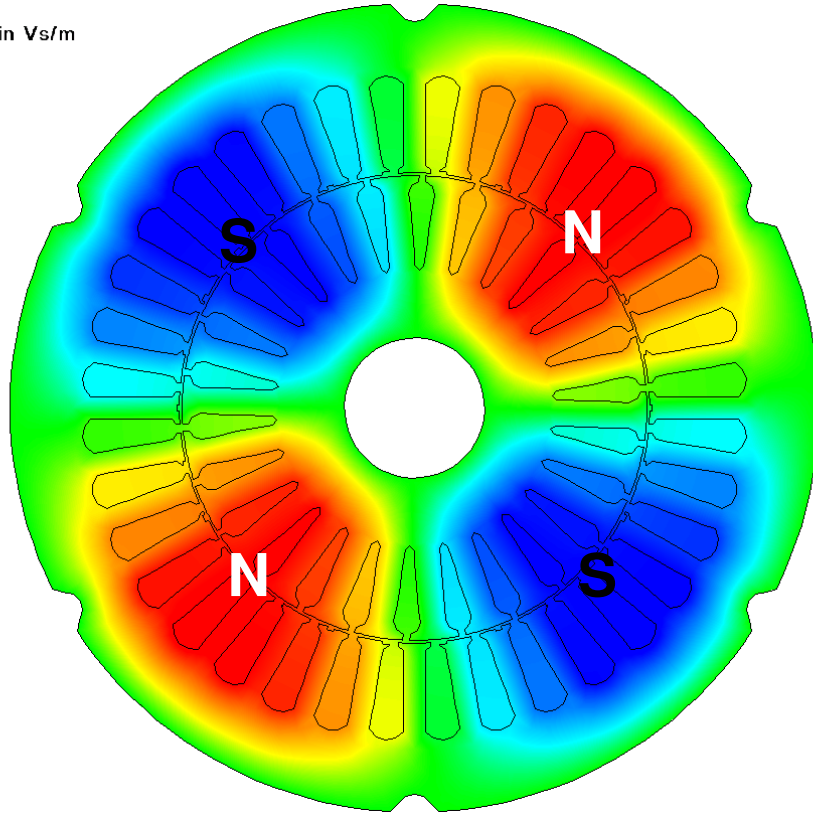
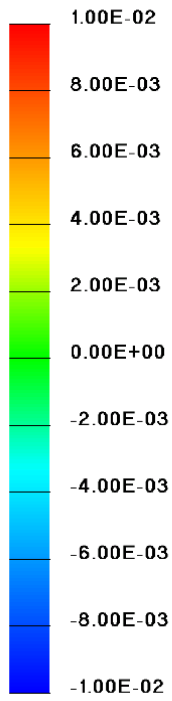
- Simulation parameters

$f_1$	48.96 Hz	stator frequency
$n$	1200 rpm	rotor speed
$I_1$	85 A	stator-phase current
$\Delta t$	243.153 ms	simulation-time step
$\Delta \alpha$	0.875 °	rotational step angle
$N$	4200	number of simulation-time steps

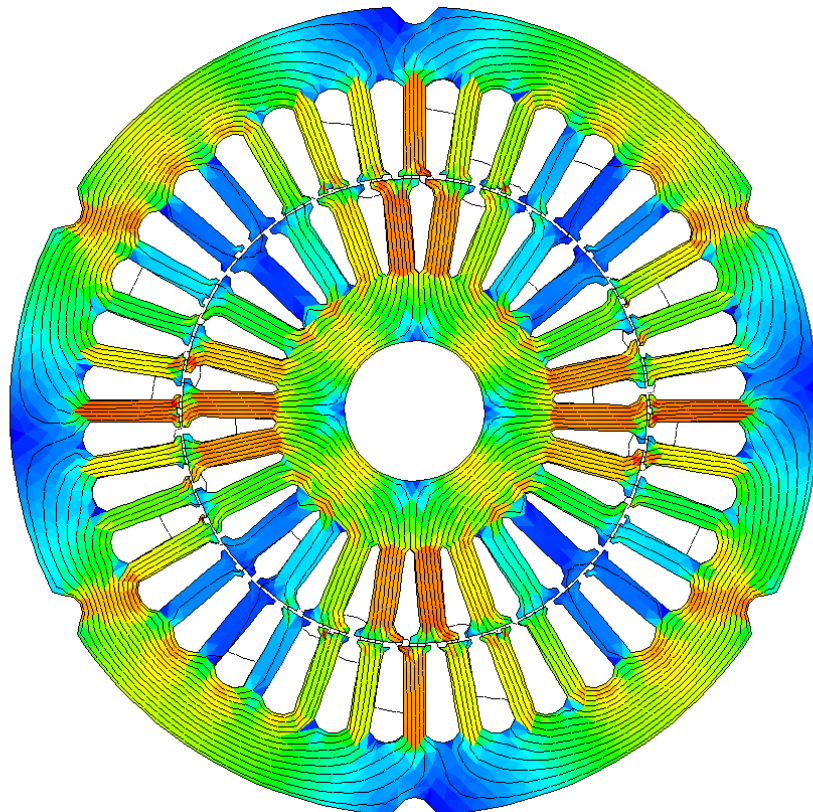
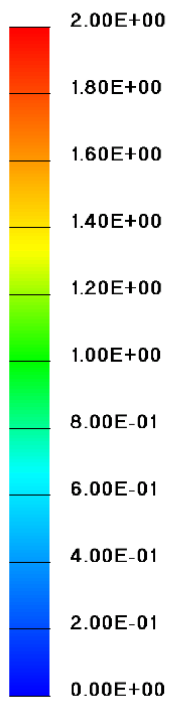
- Results from each simulation time step
  - magnetic vector potential  
 $\Rightarrow$  flux-density distribution:  $\vec{B} = \text{curl} \vec{A}$
  - derived from the flux density (Maxwell-Stress Tensor)
    - net-force  $F$
    - torque  $T$
    - surface-force density  $\sigma$



Vector Potential A in Vs/m



Flux Density B in T

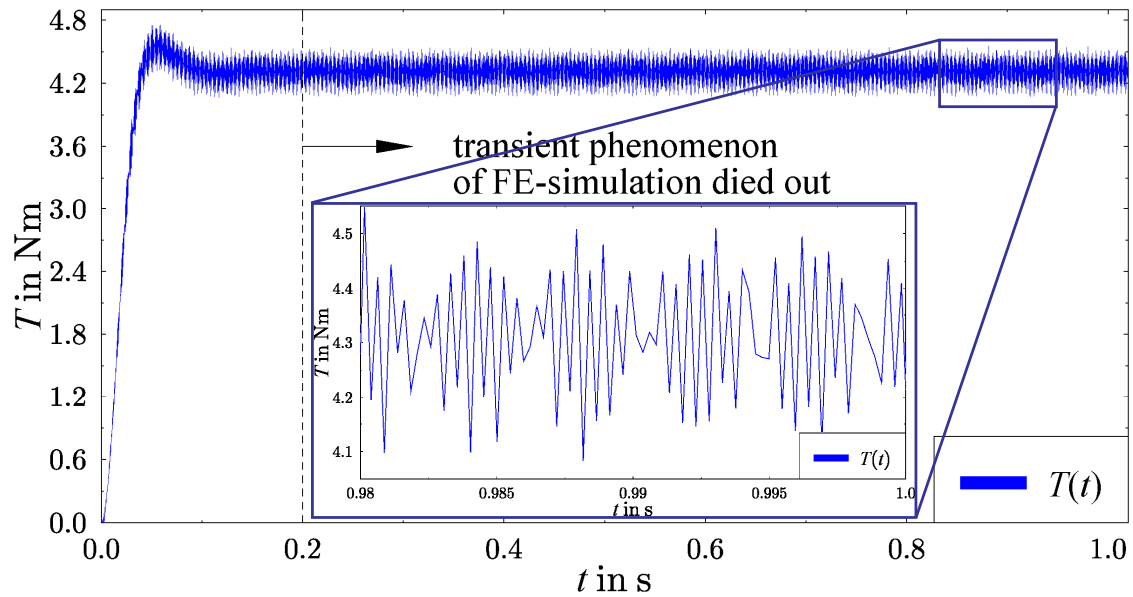




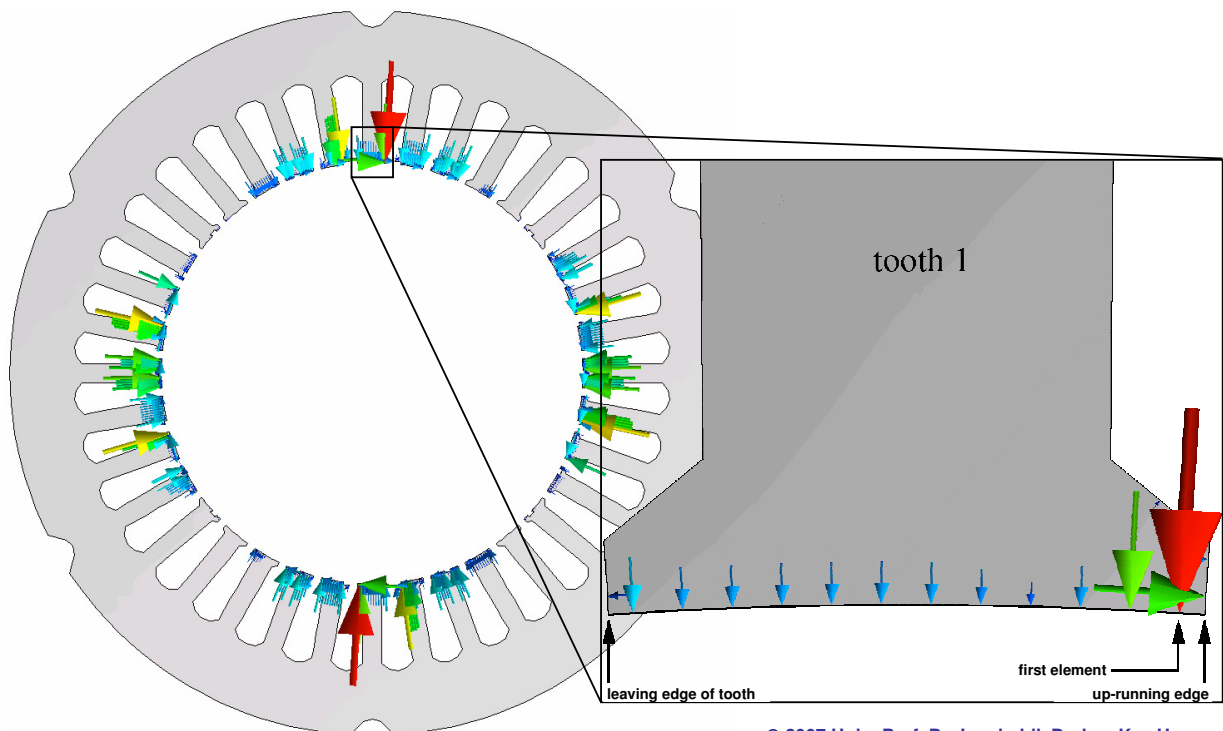


## ➤ Torque behaviour

- transient phenomenon from transient solving
- average torque:  $T = 4.31 \text{ Nm}$
- peak-to-peak torque ripple:  $\Delta T = 0.45 \text{ Nm}$



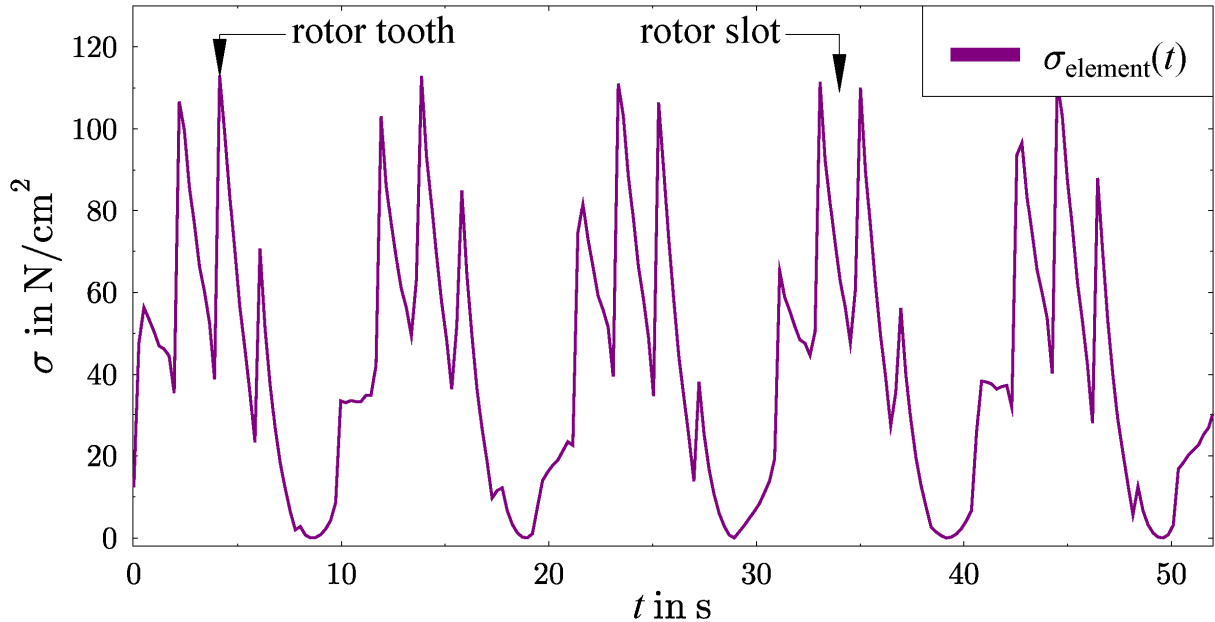
## ➤ Surface-force density derived for each time step





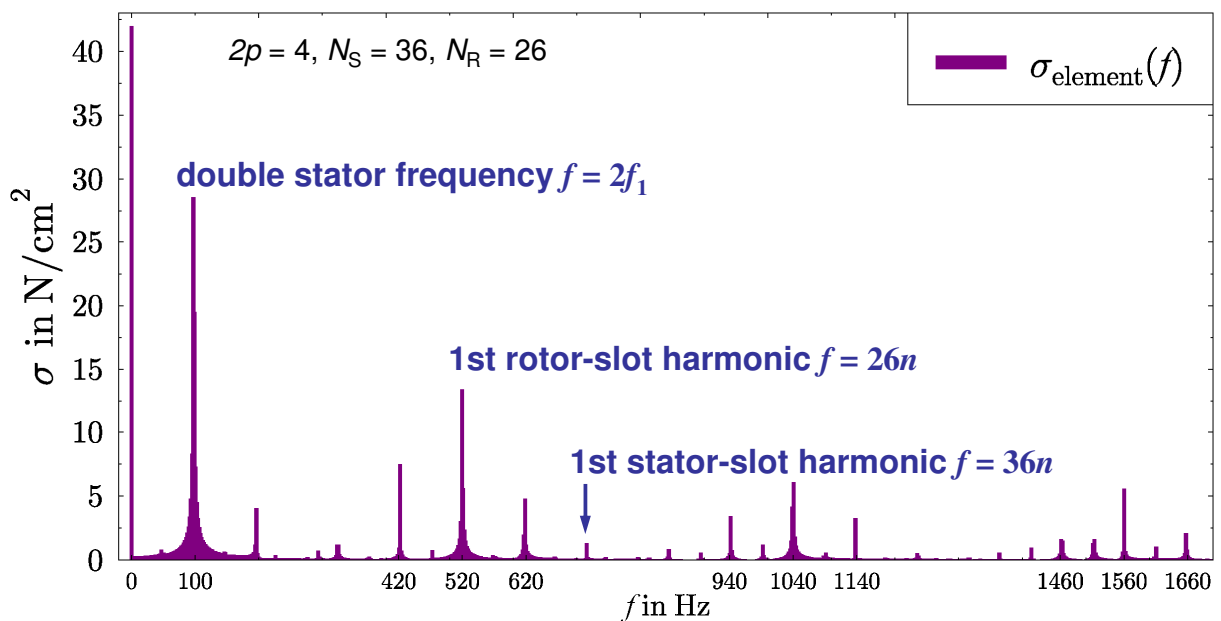
## ➤ Behaviour of surface-force density

- force pulsates, depending on  $n, N_R, N_S, f_1, p$



## ➤ Spectrum of surface-force density

- significant frequencies are selected





structure-dynamic calculation

frequency domain forces

- Example: Induction machine
- Deformation → displacement of individual nodes

$$\varepsilon = S \cdot \vec{u}$$

with  $S = \begin{bmatrix} \frac{\partial}{\partial x} & 0 & 0 & \frac{\partial}{\partial y} & 0 & \frac{\partial}{\partial z} \\ 0 & \frac{\partial}{\partial y} & 0 & \frac{\partial}{\partial x} & \frac{\partial}{\partial z} & 0 \\ 0 & 0 & \frac{\partial}{\partial z} & 0 & \frac{\partial}{\partial y} & \frac{\partial}{\partial x} \end{bmatrix}^T$



- Tension  $\sigma$  is coupled by Hooke's law with strain  $\varepsilon$

$$\sigma = H \cdot \varepsilon,$$

$$H = \frac{E(1-\mu)}{(1-\mu)(1-2\mu)} \begin{bmatrix} 1 & \frac{\mu}{1-\mu} & \frac{\mu}{1-\mu} & 0 & 0 & 0 \\ \frac{\mu}{1-\mu} & 1 & \frac{\mu}{1-\mu} & 0 & 0 & 0 \\ \frac{\mu}{1-\mu} & \frac{\mu}{1-\mu} & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & \frac{1-2\mu}{2(1-\mu)} & 0 & 0 \\ 0 & 0 & 0 & 0 & \frac{1-2\mu}{2(1-\mu)} & 0 \\ 0 & 0 & 0 & 0 & 0 & \frac{1-2\mu}{2(1-\mu)} \end{bmatrix}$$

$E$ : Young's modulus,  $\mu$ : Poisson's ratio



➤ System equation by Threshold-Accepting Method:

- potential energy

$$\Pi_p = \int_{\Omega} \boldsymbol{\varepsilon}^T H \boldsymbol{\varepsilon} d\Omega - \int_{\partial\Omega} \vec{u} \cdot \vec{\sigma}_s \boldsymbol{\varepsilon} d\partial\Omega,$$

- kinetic energy

$$T = \int_{\Omega} \frac{\rho}{2} \cdot \dot{\vec{u}} d\Omega,$$

- Lagrange function

$$L = T - \Pi_p$$

- Minimisation of Lagrange function

$$0 = \frac{d}{dt} \left( \frac{\partial L}{\partial \dot{\vec{u}}} \right) - \left( \frac{\partial L}{\partial \vec{u}} \right) + \left( \frac{\partial F}{\partial \dot{\vec{u}}} \right),$$

- $F$  is the damping



➤ Discretisation results in the differential equation of motion:

$$K \cdot D + C \cdot \dot{D} + M \cdot \ddot{D} = F.$$

K: global stiffness matrix

D: vector of nodal deformation

C: damping matrix

M: mass matrix

F: exciting force matrix

➤ Time derivative

$$\dot{D} = \frac{dD}{dt} = j\omega D$$

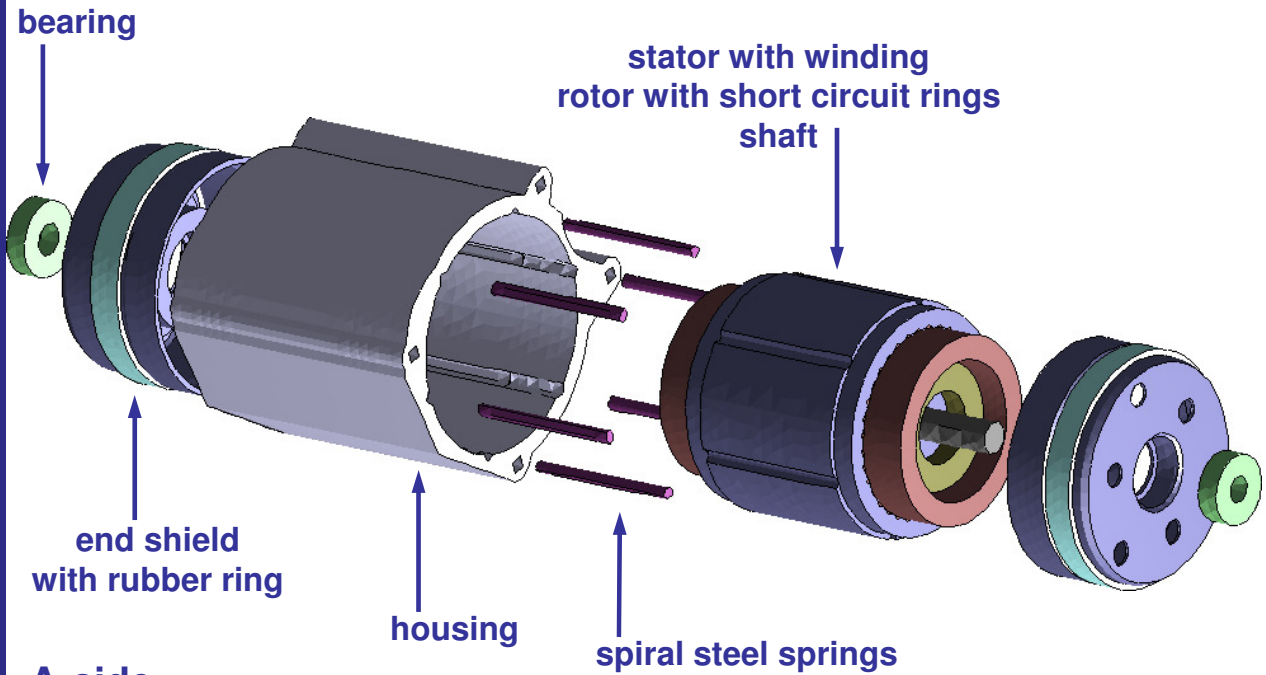
⇒

$$(K + j\omega C - \omega^2 M) \cdot D = F.$$



## ➤ Mechanical model

B-side



A-side

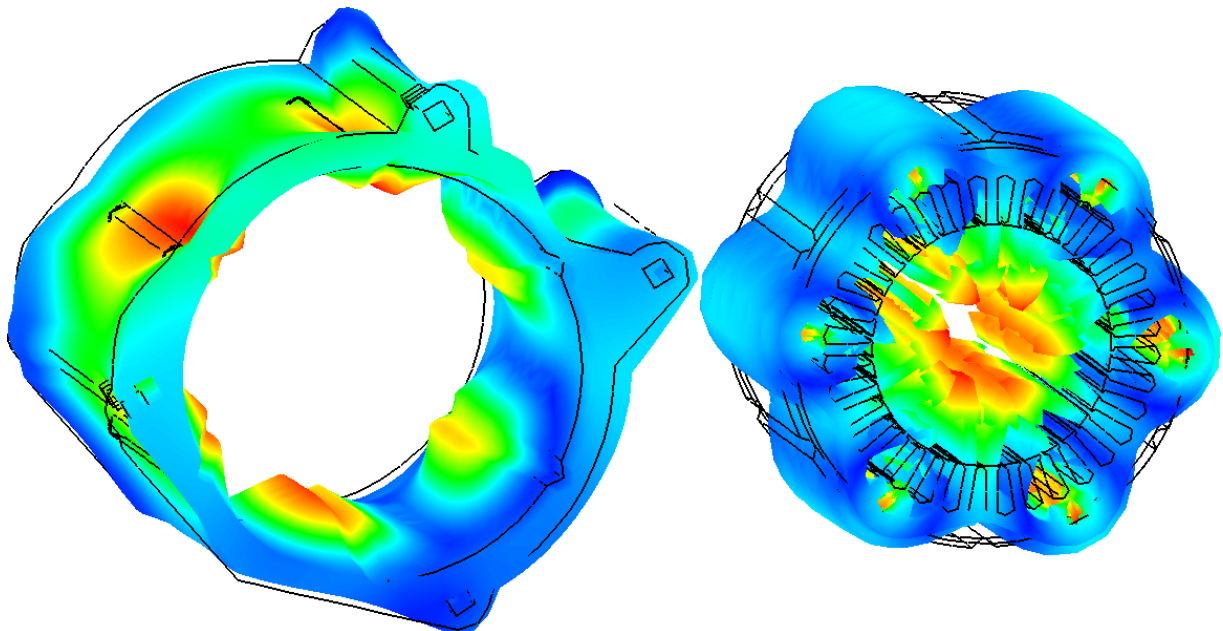
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## ➤ Simulation result

- ⇒ deformation of entire machine in frequency domain
- ⇒ example deformation at  $t = 0$  for  $f = 618$  Hz



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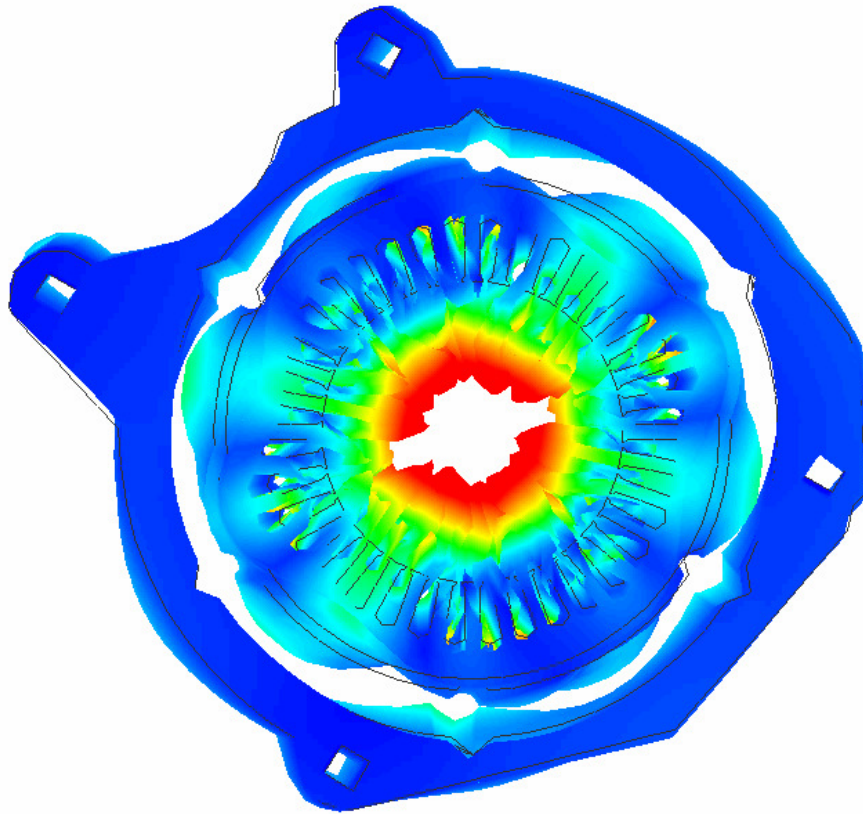
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## Structure-dynamic calculation

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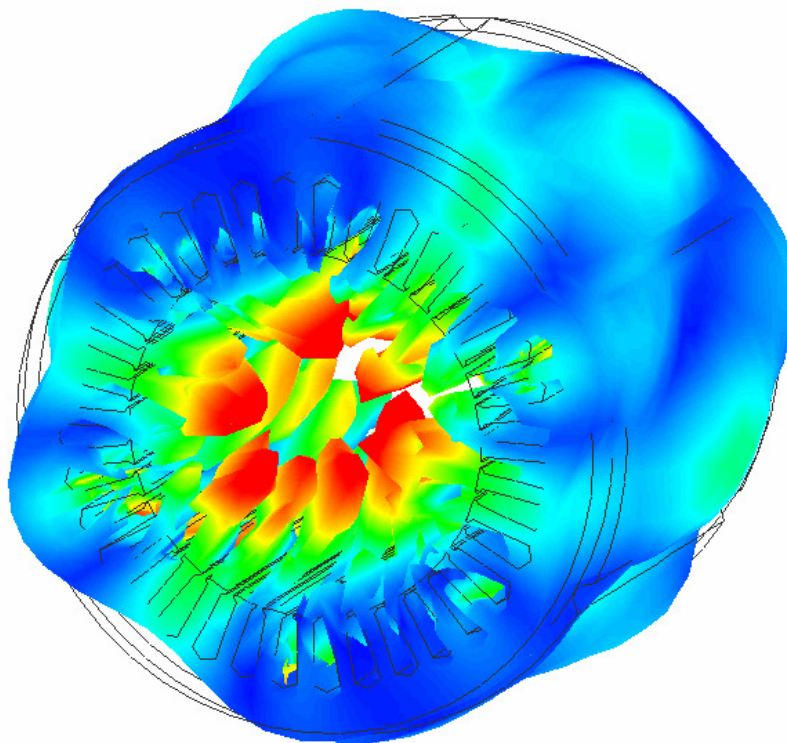


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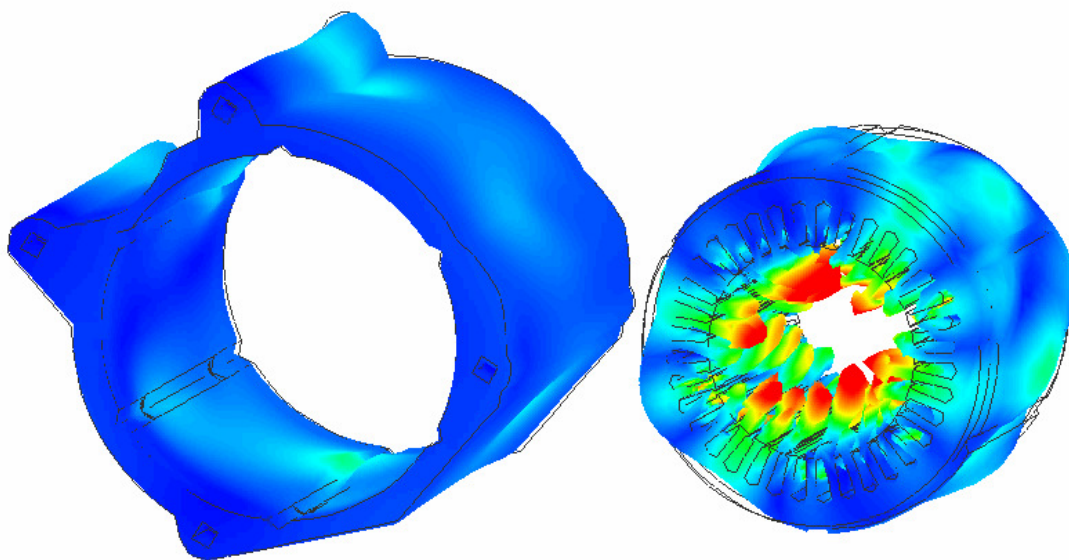
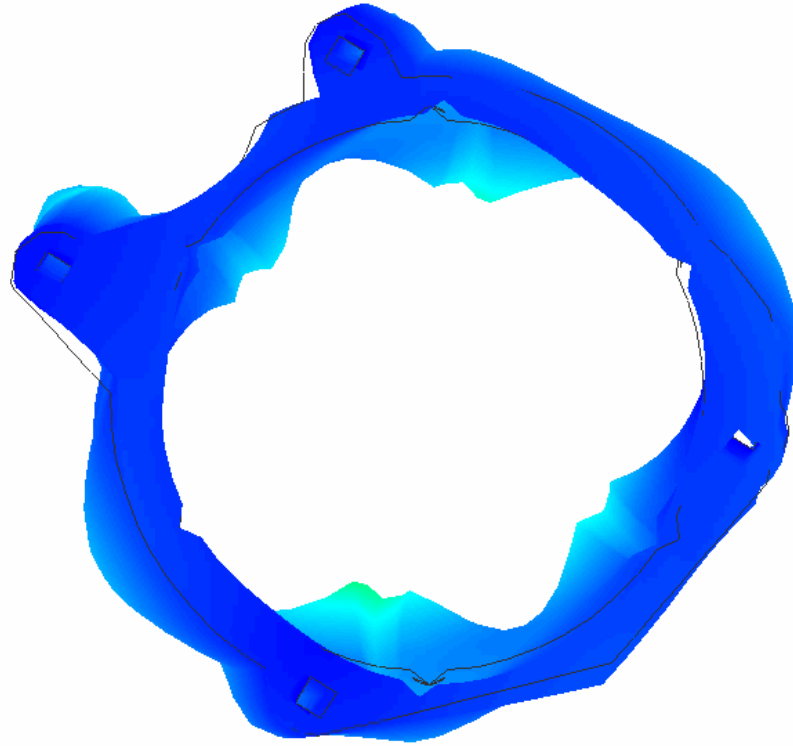


## Structure-dynamic calculation

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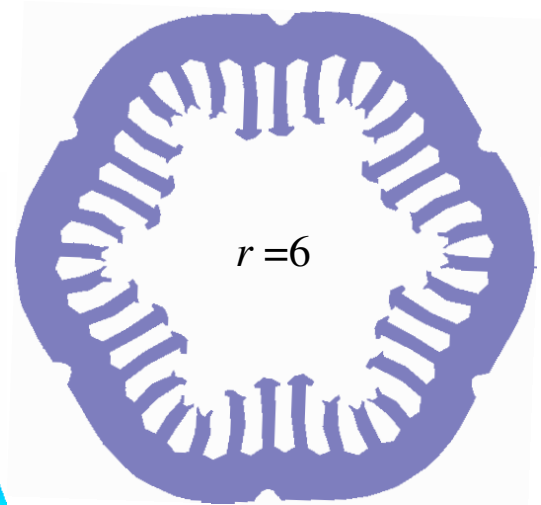
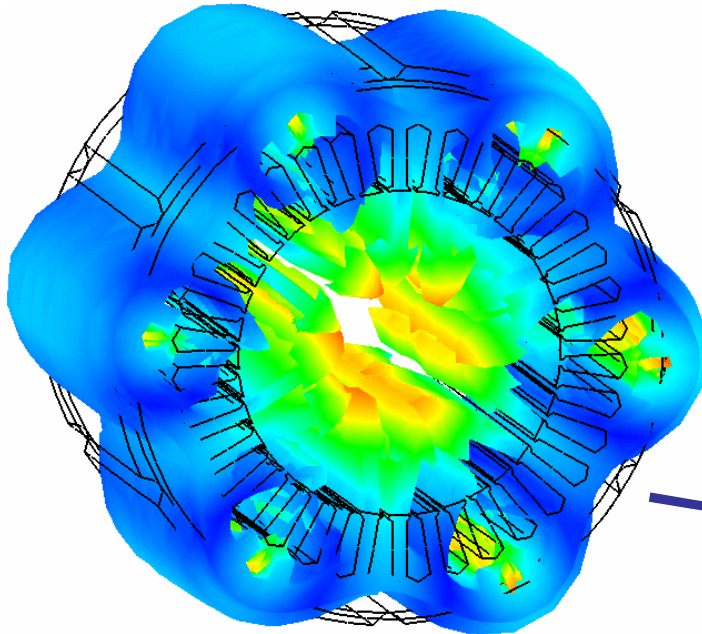


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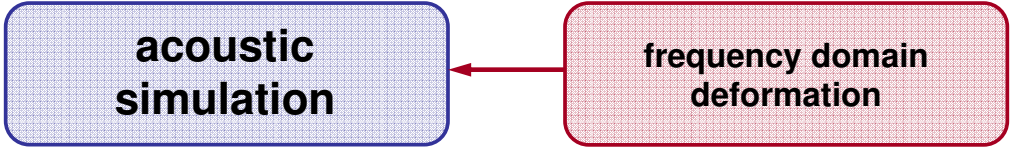


- Analysis of the deformation:
  - modes of deformation  $r$
  - body-sound index  $L_{BSI}$
- Example: mode analysis



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- Three sources for acoustic noise:
  - broad band fan and ventilation noise (500 - 1000 Hz)
  - single tones from the bearings > 3000 Hz
  - vibration and oscillations excited by electromagnetic forces
    - single tones in the entire audible spectrum
- Acoustic simulation considers electromagnetically excited vibration as noise source

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- Acoustic noise:
  - vibration is decoupled from the surface of the machine  
⇒ Boundary Element Method (BEM)

- Sound pressure derived from Helmholtz equation:

$$\Delta \underline{p} + k^2 \cdot \underline{p} = 0$$

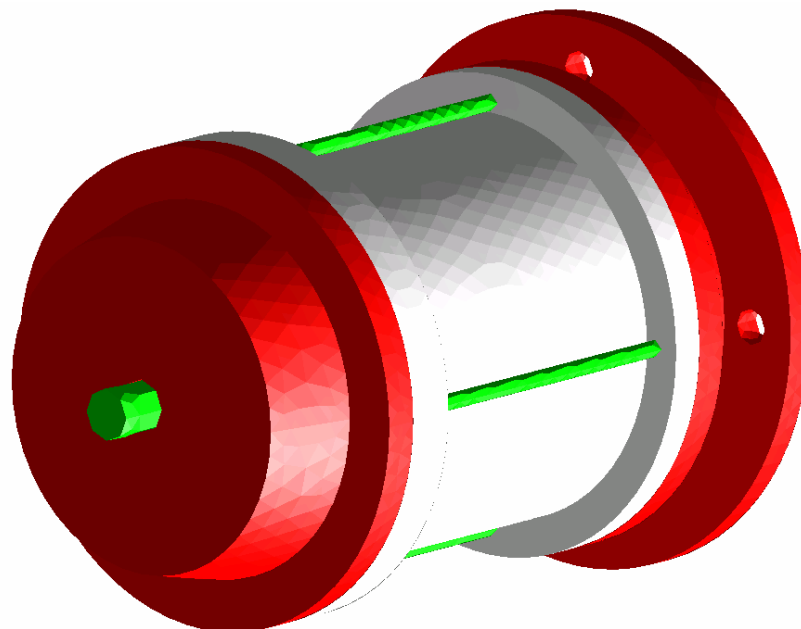
- Discretisation results in the system equation for solving:

$$H \cdot \underline{p} = G \cdot \vec{v}.$$

$H$  and  $G$  are system matrices and  $v$  the vector of the local surface velocity



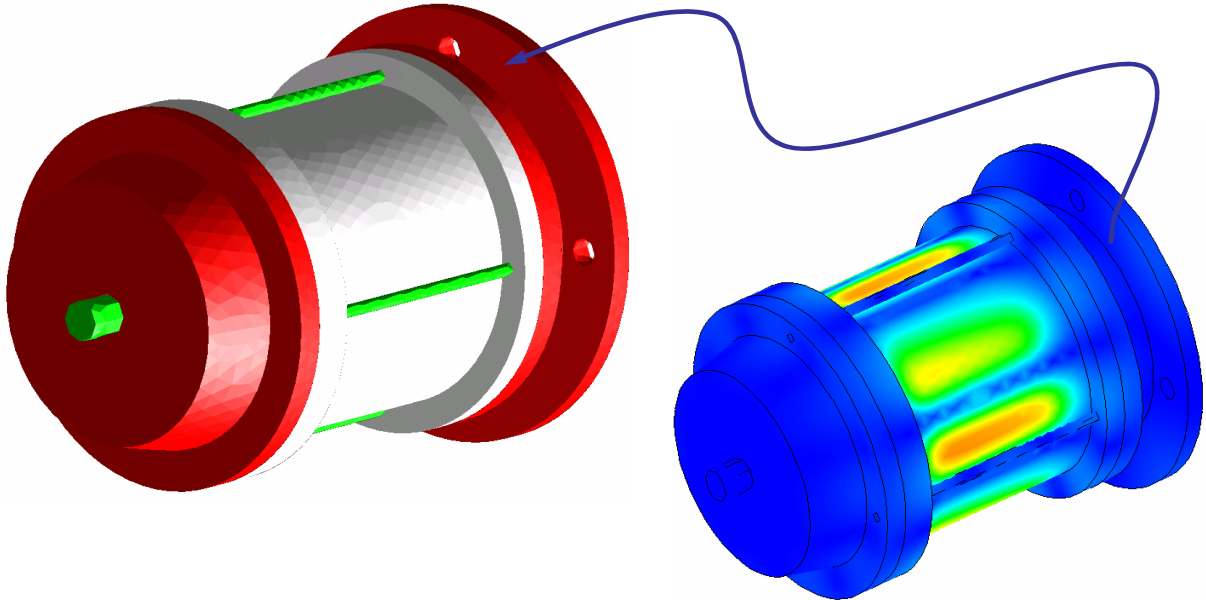
- Example for acoustic simulation:  
Switched Reluctance Motor (SRM)
- Model consists only of exterior surface of the SRM







- Deformation is transformed from the mechanical model onto the surface of the acoustic model



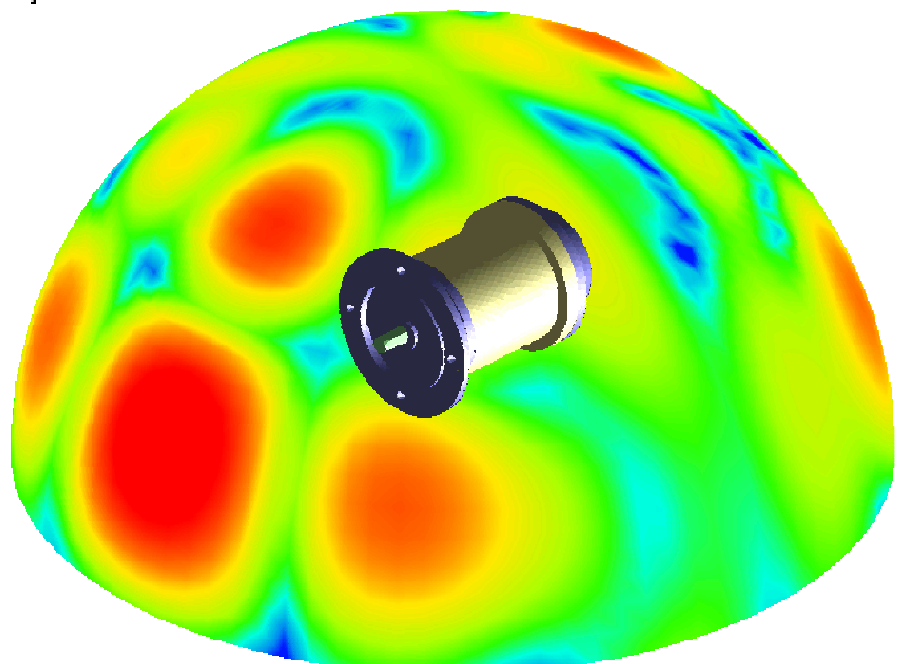
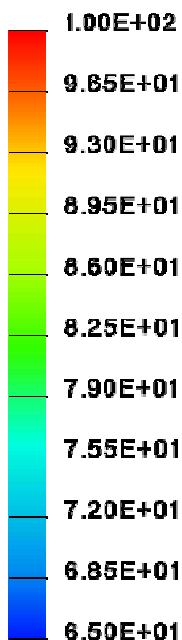
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- Acoustic sound pressure is calculated on an analysis surface, e.g. a sphere (1 m distance from surface of SRM)

sound pressure [dB]



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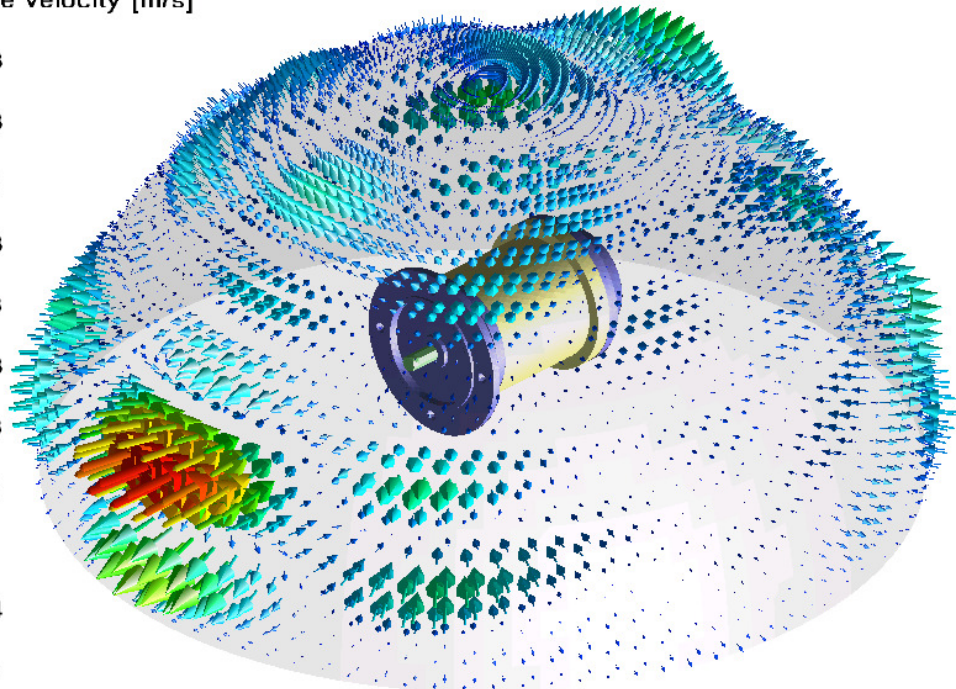
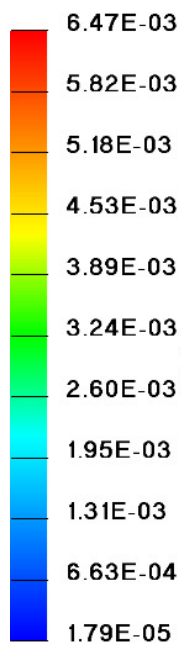
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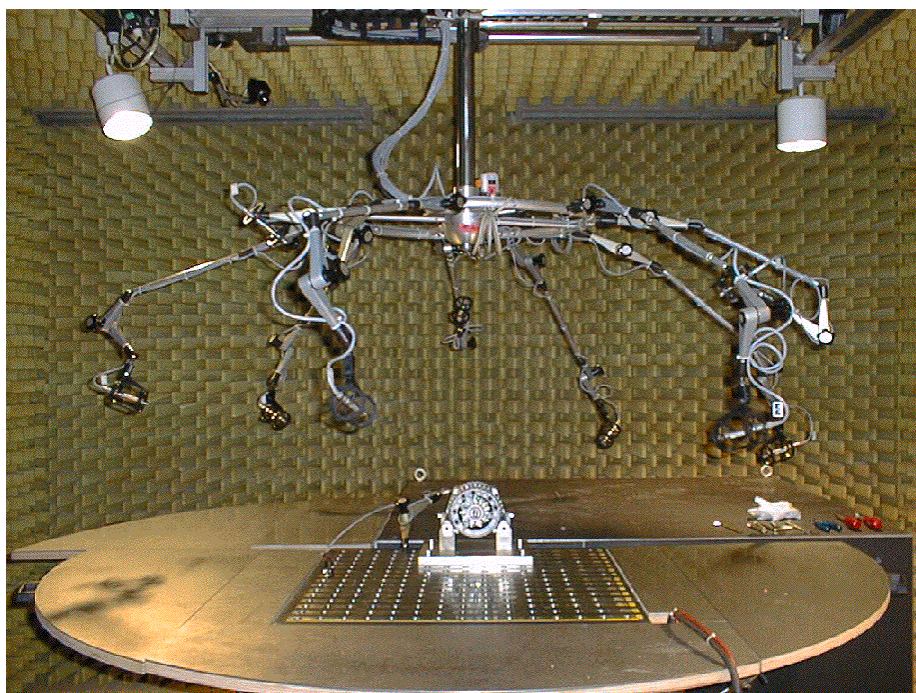
➤ From  $p$  the sound particle velocity is derived

sound particle velocity [m/s]



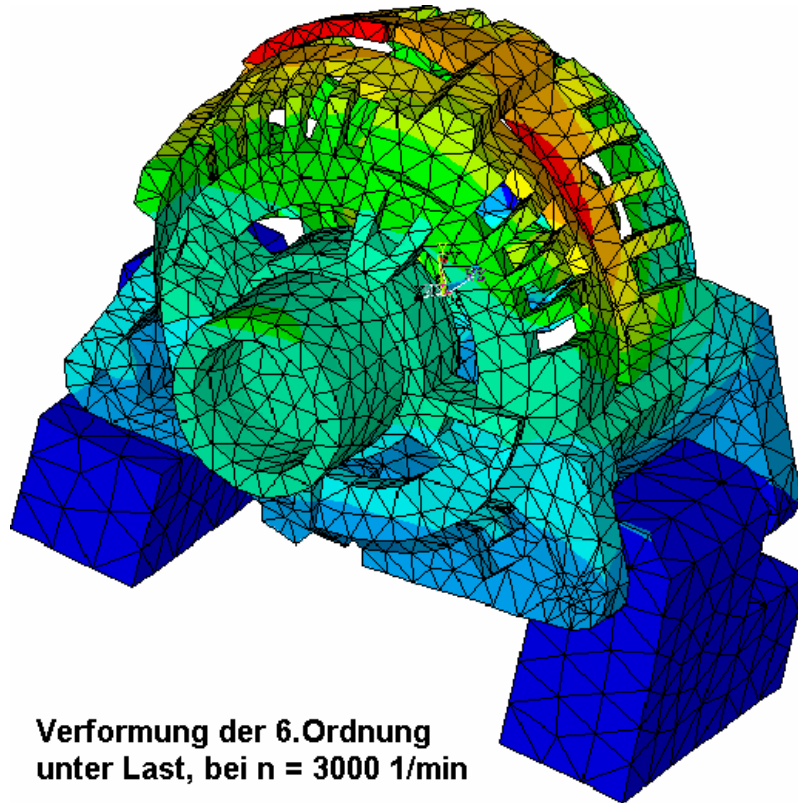
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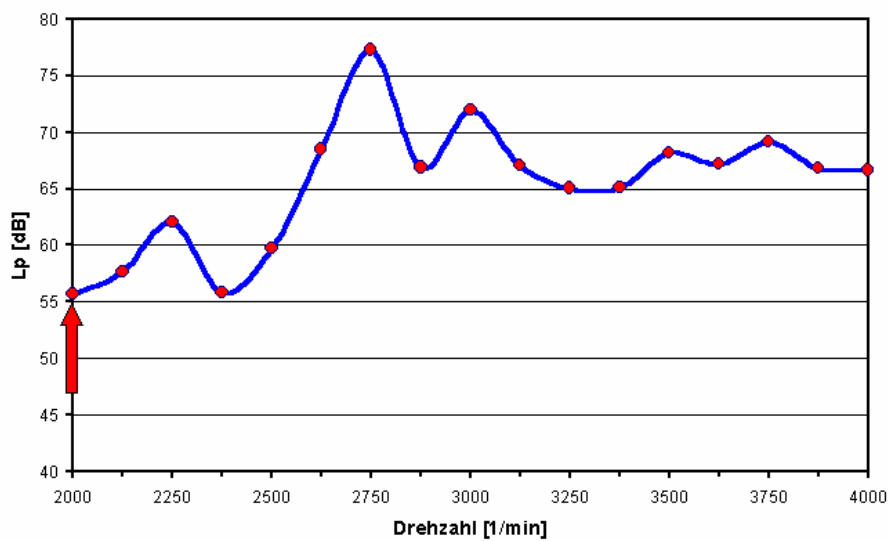
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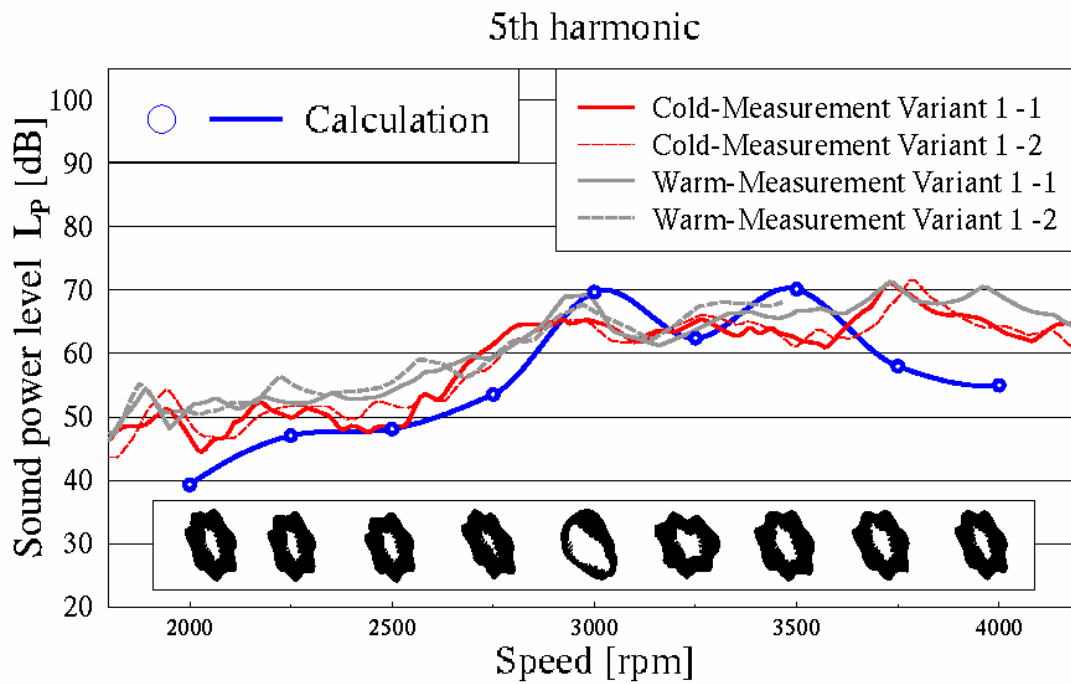


Verformung der 6. Ordnung unter Last, bei  $n = 3000$  1/min



Schalleistungspegel der 5. und 6. Ordnung [dB]





- Numerical simulation
  - **consideration** of structure-dynamic and acoustic behaviour of electrical machines **a-priori** during design
  - examples of IM and SRM show potential
- Presented method
  - **designed** to be used for **any electrical machine**
  - **verification** by measurement is possible
- Structured analysis
  - **consideration** of manufacturing **faults**
  - **optimisation** of materials and electrical values